Question 1

(i)	x 6 17 9 20 13 15 11 14	M1 for attempt at	
	y 6 13 10 11 9 7 12 15	ranking (allow all	
	Rank x 8 2 7 1 5 3 6 4	ranks reversed)	
	Rank y 8 2 5 4 6 7 3 1	M1 for d^2	
	d 0 0 2 -3 -1 -4 3 3	WIT IOI <i>a</i>	
	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		
	$\Sigma d^2 = 48$	A1 CAO for Σd^2	
	$r_s = 1 - \frac{6\Sigma d^2}{n(n^2 - 1)} = 1 - \frac{6 \times 48}{8 \times 63}$	M1 for method for r_s	
	= 0.429 (to 3 s.f.) [allow 0.43 to 2 s.f.]	A1 f.t. for $ r_s < 1$ NB No ranking scores zero	5
(ii)			
	H_0 : no association between X and Y in the population	B1 for H ₀	
	H_1 : some positive association between X and Y in the	B1 for H ₁	
	population	B1 for population SOI	3
		NB $H_0 H_1 \underline{\text{not}}$ ito ρ	
	One tail test critical value at 5% level is 0.6429	B1 for ± 0.6429	
	Since $0.429 < 0.6429$, there is insufficient evidence to reject H_0 ,	M1 for sensible comparison with	
		c.v., provided that $ r_s < 1$	
	i.e. conclude that there is not enough evidence to show	A1 for conclusion in	
	positive association between the two judges' scores.	context f.t. their r_s	
		and sensible cv	3
(iii)	A bivariate Normal distribution is required.	B1	
	Scatter diagram.	G1 labelled axes	
	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	G1 correct points	
	Suitable discussion	E1	
		E1	5
		TOTAL	16

## **Question 2**

_		1	
(i)	Counts have a uniform average rate of occurrence	E1	2
	All counts are independent	E1	
(ii)	Variance = 3.4	B1	1
(iii)	(A) Either $P(X = 3) = 0.5584 - 0.3397 = 0.2187$ Or $P(X = 3) = e^{-3.4} \frac{3.4^3}{3!} = 0.2186$ (B) Using tables: $P(X \ge 3) = 1 - P(X \le 2)$	M1 for use of tables or calculation A1 M1 for 1 - $P(X \le 2)$	2
	= 1 - 0.3397 $= 0.6603$	M1 correct use of Poisson tables A1	3
(iv)	$\lambda = 12 \times 3.4 = 40.8$ $P(X = 40) = e^{-40.8} \frac{40.8^{40}}{40!} = 0.0625$	B1 for mean M1 for calculation A1	3
(v)	Mean no. per hour = $12 \times 3.4 = 40.8$ Using Normal approx. to the Poisson, $X \sim N(40.8, 40.8)$ $P(X \ge 40) = P\left(Z > \frac{39.5 - 40.8}{\sqrt{40.8}}\right)$ $= P(Z > -0.2035) = \Phi(0.2035)$ $= 0.5806$	B1 for Normal approx. B1 for correct parameters (SOI) B1 for correct continuity corr. M1 for probability using correct tail A1 CAO (3 s.f.)	5
(vi)	Overall mean = 4.8 $P(X \ge 8) = 1 - P(X \le 7)$ $= 1 - 0.8867 = 0.1133$	B1 for 4.8 M1 A1	3
		TOTAL	19

## **Question 3**

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Que	SHOIL 2		
(i)	(A) $P(X < 65) =$ $P\left(Z < \frac{65 - 63}{5.2}\right)$ $= P(Z < 0.3846)$ $= \Phi(0.3846) = 0.6497$ (B) $P(60 < X < 65) = P\left(\frac{60 - 63}{5.2} < Z < \frac{65 - 63}{5.2}\right)$ $= P(-0.5769 < Z < 0.3846)$ $= \Phi(0.3846) - (1 - \Phi(0.5769))$ $= 0.6497 - (1 - 0.7181)$ $= 0.3678$	M1 for standardizing M1 for structure A1 CAO (min 3 s.f.), NB When a candidate's answers suggest that (s)he appears to have neglected to use the difference column of the Normal distribution tables penalise the first occurrence only M1 for standardizing both M1 for correct structure A1 CAO 3s.f.	3 3
(ii)	P(All 5 between 60 and 65) = $0.3678^5 = 0.00673$	M1 A1 FT (min 2sf)	
			2
(iii)	From tables $\Phi^{-1}(0.95) = 1.645$ $\frac{k - 63}{5.2} = -1.645$ $x = 63 - 5.2 \times 1.645 = 54.45 \text{ mins}$	B1 for ±1.645 seen M1 for correct equation in k A1 CAO	3
(iv)	H ₀ : $\mu = 63$ minutes; H ₁ : $\mu < 63$ minutes. Where $\mu$ denotes the population mean time on the new course. Test statistic = $\frac{61.7 - 63}{5.2/\sqrt{15}} = \frac{-1.3}{1.3426}$ = -0.968	B1 for use of 63 B1 for both correct B1 for definition of $\mu$ M1 must include $\sqrt{15}$	3
	5% level 1 tailed critical value of $z = 1.645$ -0.968 > -1.645 so not significant. There is not sufficient evidence to reject H ₀	B1 for ±1.645 M1 for sensible comparison leading to a conclusion  A1 FT for correct	
	course results in lower times.	conclusion in words in context	5 19

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## Question 4

	H ₀ : no association between category of runner and type of				B1	1
(i)	running;	. 1	C	1 .		
	$H_1$ : some association between category of runner and type					
	of running;					
					M1 A2 for expected	
	EXPECTED	Junior	Senior	Veteran	values (to 2 dp)	
	Track	5.13	7.84	6.03	(allow A1 for at least	
	Road	6.48	9.90	7.62	one row or column	
	Both	5.40	8.25	6.35	correct)	
					correct)	
	CONTRIBUTN	Junior	Senior	Veteran	2.51.6	
	Track	2.9257	0.0032	2.6949	M1 for valid attempt at	
	Road	0.9468	0.3663	2.5190	$(O-E)^2/E$	
	Both	0.3615	0.3694	0.0192	A1 for all correct  NB These M1A1 marks cannot be implied by	
					a correct final value of $X^2$	
	2				M1 for summation	7
	$X^2 = 10.21$				A1 for $X^2$	
					AT IOI A	
	Refer to $X_4^2$				B1 for 4 deg of f	
	a		0.400		B1 CAO for cv	
	Critical value at 5% level = 9.488  Result is significant					
					B1 FT their 'sensible'	
	result is signific	zam			$X^2$	
	There is evide				E1 must be consistent	
	association between category of runner and type of running.  NB if H ₀ H ₁ reversed, or 'correlation' mentioned, do not award				f E1 must be consistent	
					with their $X^2$	4
	NB if $H_0$ $H_1$ reverse first B1or final E1	ed, or 'correlat	ion' mentioned, d	o not award		
(ii)	mst B101 imai E1					
(11)	<ul> <li>Juniors a</li> </ul>	ppear be tra	ck runners mo	re often	E1 E1	
	<ul> <li>Juniors appear be track runners more often than expected and road less often than expected.</li> <li>Seniors tend to be as expected in all three categories of running.</li> <li>Veterans tend to be road runners more than expected and track runners less than expected.</li> </ul>				ET ET	
					E1 E1	
					E1 E1	6
					TOTAL	18